

➤ Random forest for network inference (in biology)

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SFds

ECAS-SFds course on random forest
Fréjus (France), October 8-13, 2023



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Mathematical object used to model **relational data between entities**.

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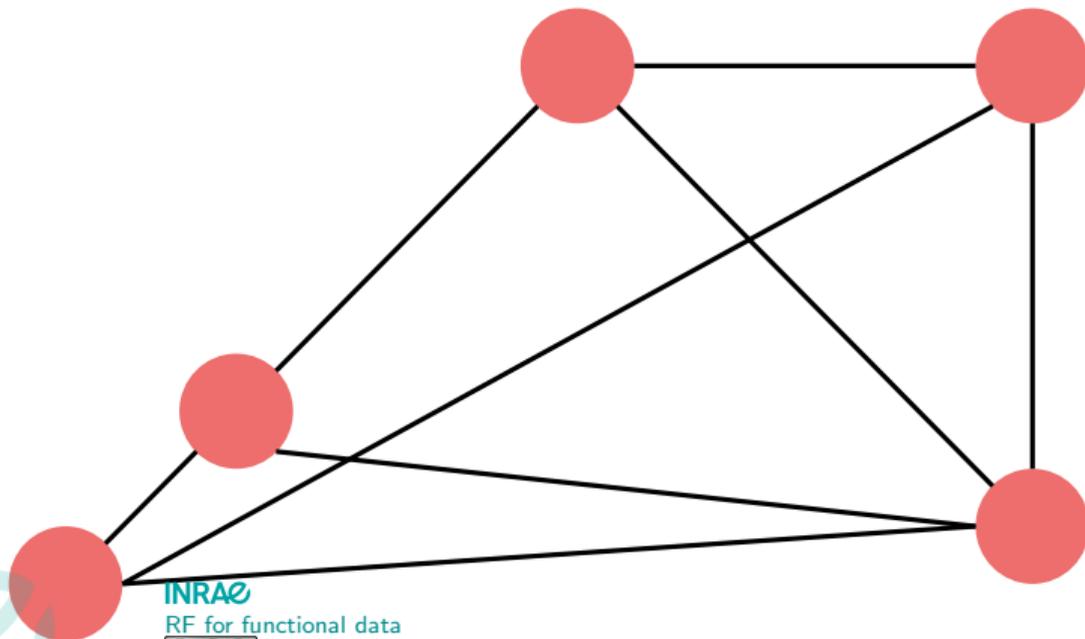
The entities are called the nodes or the vertices



> What is a network/graph?

Mathematical object used to model **relational data between entities**.

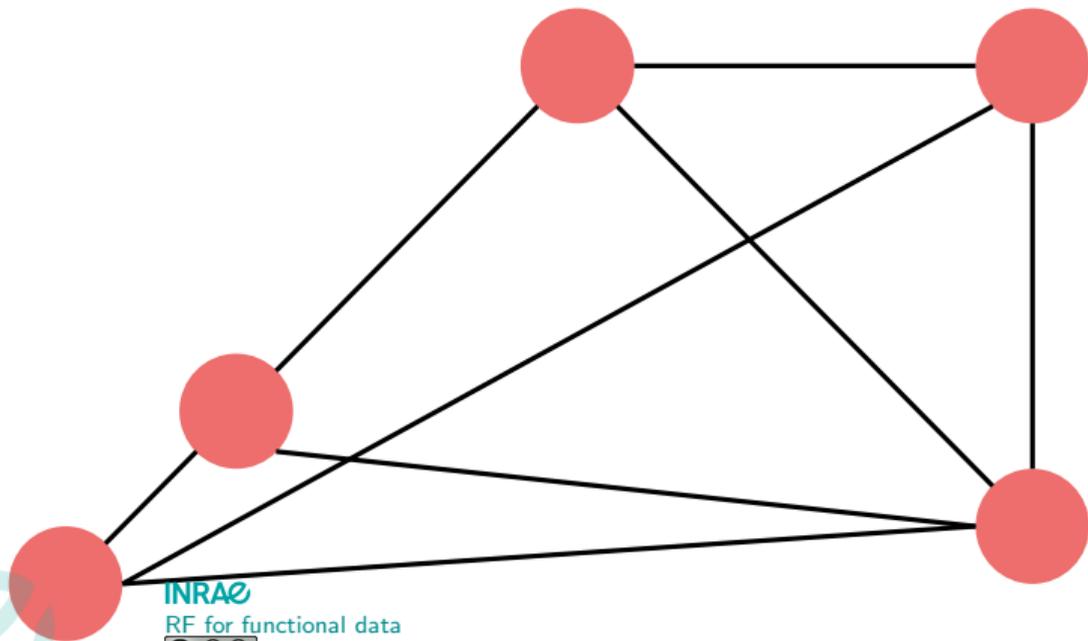
A relation between two entities is modeled by an **edge**



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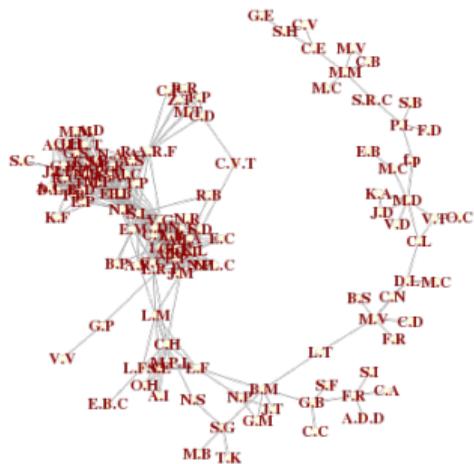
Mathematical object used to model relational data between entities.

A relation between two entities is modeled by an edge + edges can even be oriented



➤ (non biological) Examples

Social network: nodes: persons - edges: 2 persons are connected (“friends”)



(Natty's facebook¹ network)



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RF for functional data



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➤ (non biological) Examples

Modeling a large corpus of medieval documents

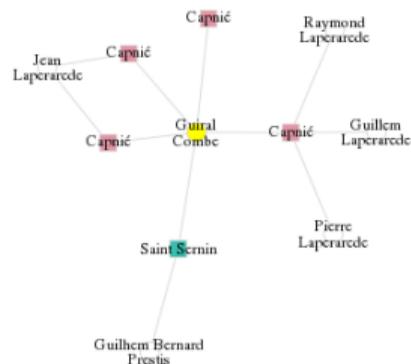


Notarial acts (mostly “baux à fief”, more precisely, land charters) established in a “seigneurie” named “Castelnau Montratier”, written between 1250 and 1500, involving tenants and lords.^a

^a<http://graphcomp.univ-tlse2.fr>

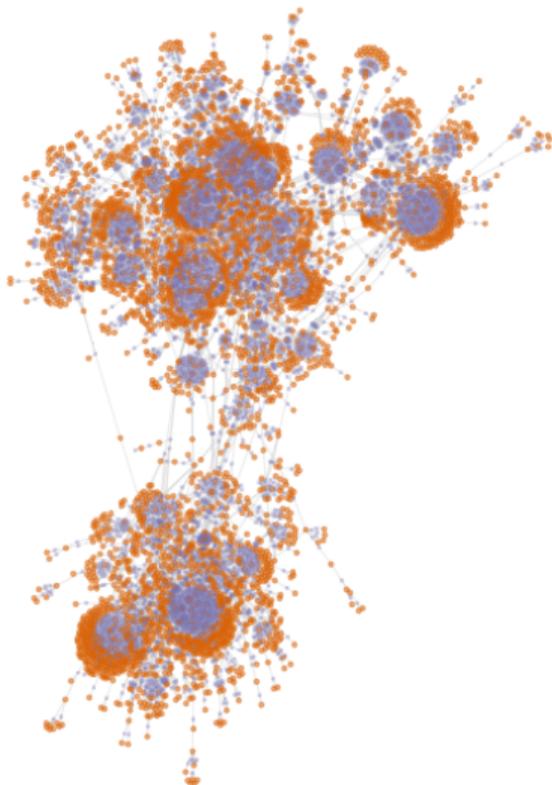
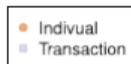
➤ (non biological) Examples

Modeling a large corpus of medieval documents



- ▶ nodes: transactions and individuals (3 918 nodes)
- ▶ edges: an individual is directly involved in a transaction (6 455 edges)

> (non biological) Examples



> Standard issues associated with networks

Inference

Given data, how to build a graph whose edges represent the “dependency relationship” between variables?



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Graph mining (examples)

1. Network visualization
2. Network clustering



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Inference

Given data, how to build a graph whose edges represent the “dependency relationship” between variables? **Random forest is useful here!**

Graph mining (examples)

1. Network visualization
2. Network clustering



Network inference in biology: an overview

From GGM to random forest

Variants of network inference with random forest

More on tree ensemble methods



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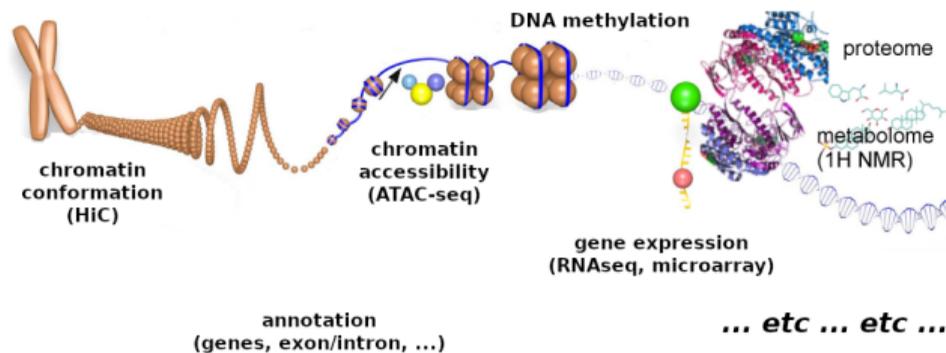
RF for functional data



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➤ Cell molecular mechanisms: gene transcription/translation

Disclaimer: This is way more complicated than what I will tell...!



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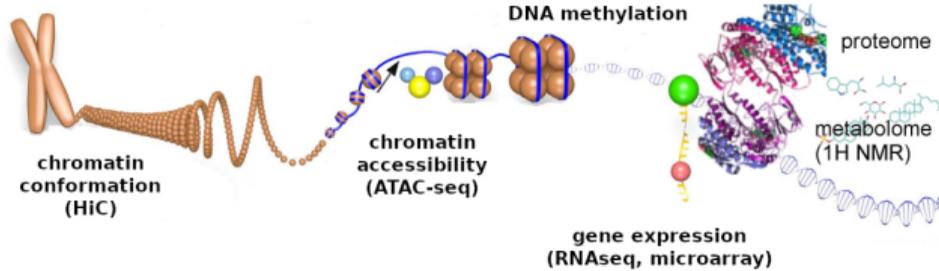
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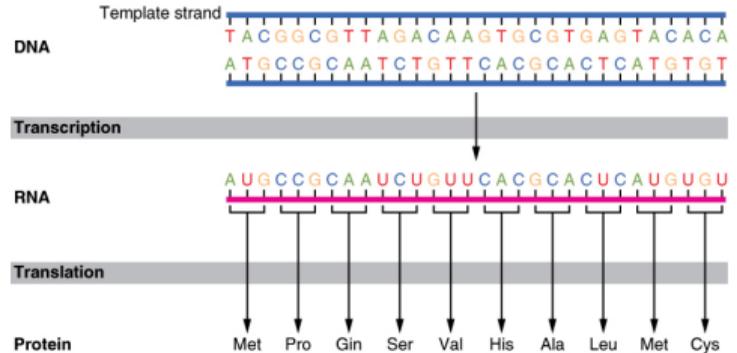
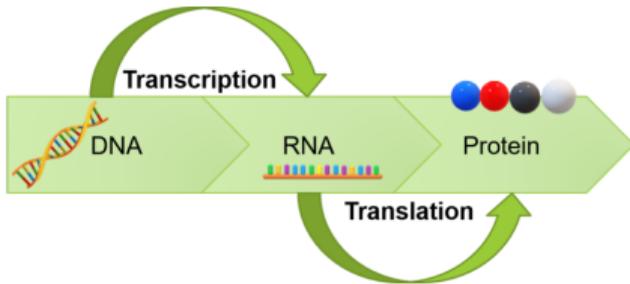
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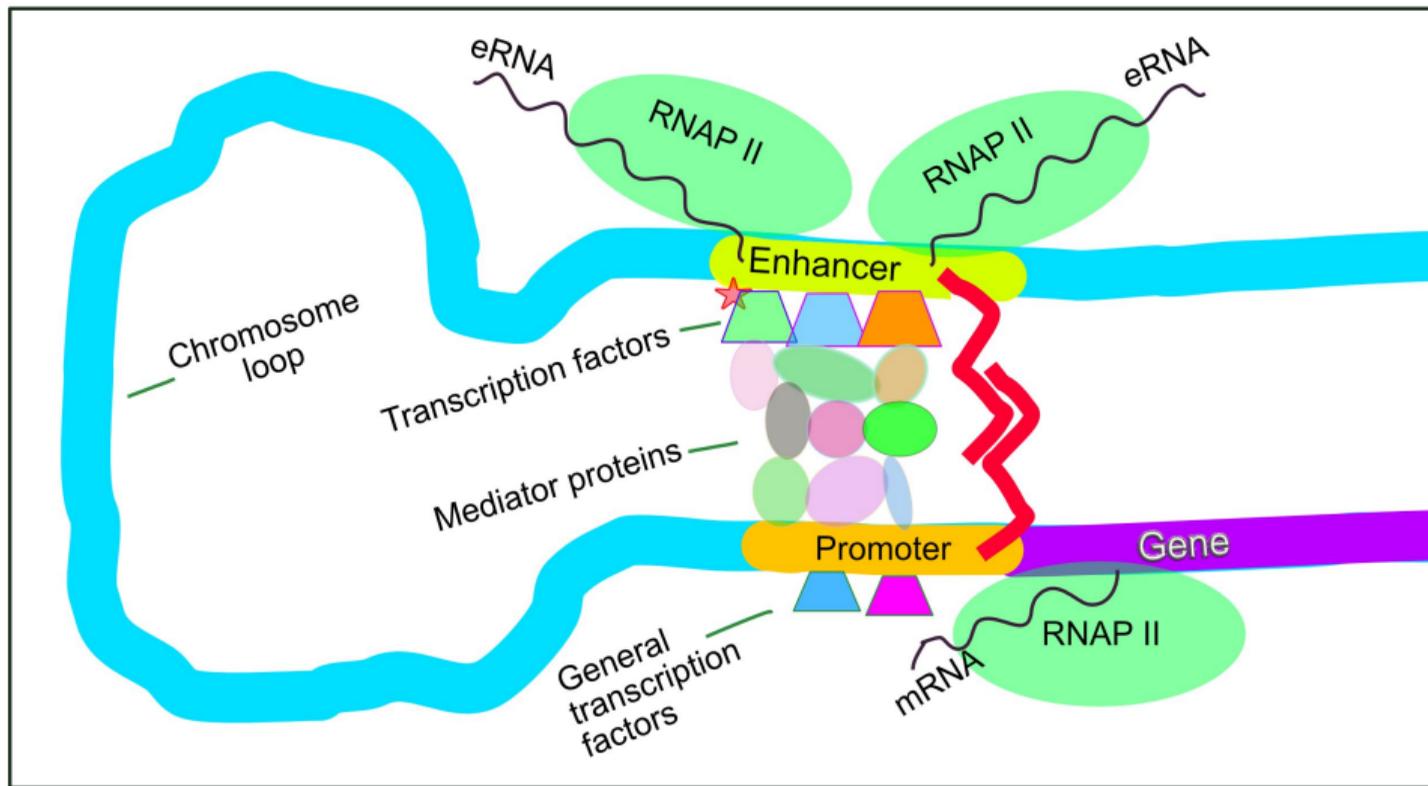
annotation (genes, exon/intron, ...)

... etc ... etc ...





Cell molecular mechanisms: (gene-)gene regulation



> In short: gene networks

What we would like: use data on gene expression to obtain a network with:

- ▶ nodes = genes
- ▶ edge = a regulation process of one gene on the other gene

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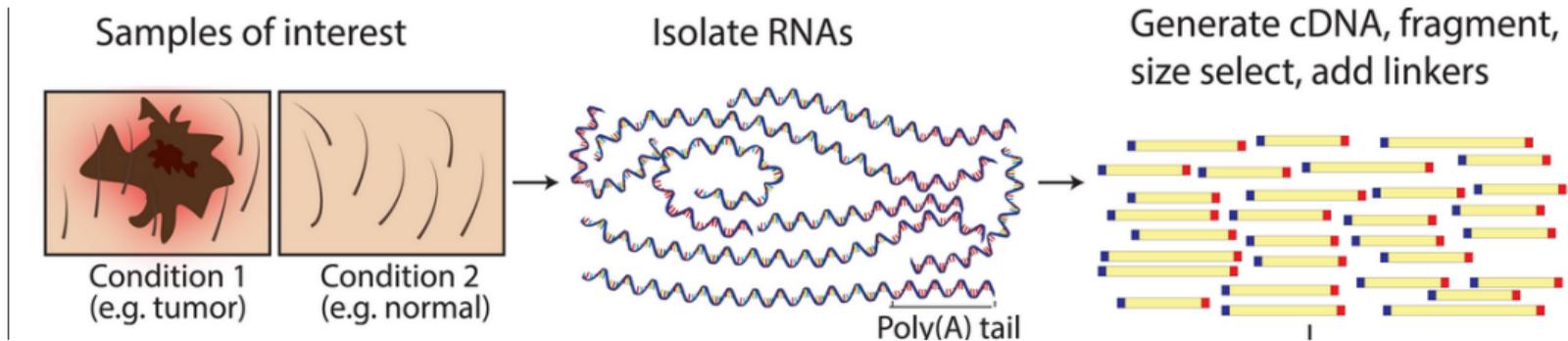
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What we approximately actually obtain:

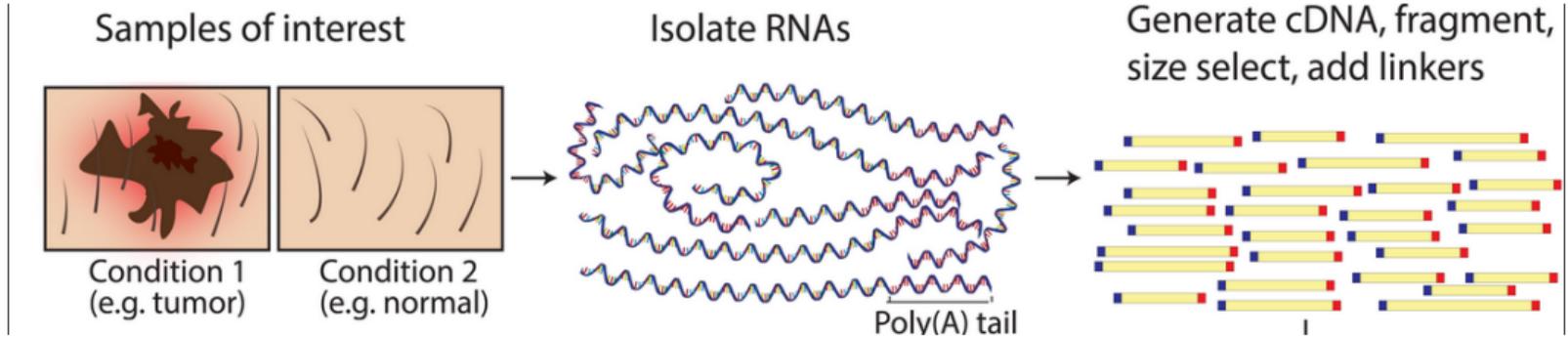
- ▶ nodes = genes
- ▶ edge = the fact that two genes show similar patterns of expression



Collecting data: gene expression



Collecting data: gene expression



Various techniques:

- ▶ continuous data: RT-qPCR, various arrays
- ▶ count data: RNA-seq (and its single-cell variant)



➤ Back to a more formal (less biology) description

Data: large scale gene expression data

$$\begin{array}{l} \text{individuals} \\ n \simeq 30/50 \end{array} \left\{ X = \begin{pmatrix} \cdot & \cdot & \cdot & \cdot & \cdot & \cdot \\ \cdot & \cdot & X_i^j & \cdot & \cdot & \cdot \\ \cdot & \cdot & \cdot & \cdot & \cdot & \cdot \end{pmatrix} \right.$$

variables (genes expression), $p \simeq 10^{3/4}$

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Note: This is hard to perform genome-widely: Humans $\geq 20,000$ genes coding for proteins (plus the others), *Bacillus subtilis* $\sim 4,000$ genes



➤ Main methods used for network inference

- ▶ Relevance network: correlation, mutual information
- ▶ Partial correlation (Gaussian Graphical Model framework)
- ▶ Bayesian network
- ▶ Other regression based methods, including:
 - ▶ random forest: best in [Marbach et al., 2012] / DREAM4 challenge!
 - ▶ (of course) deep learning
 - ▶ ...



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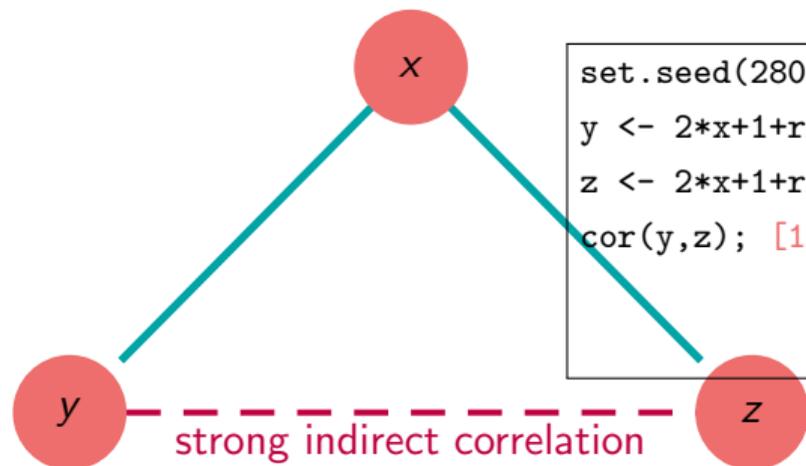
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RF for functional data



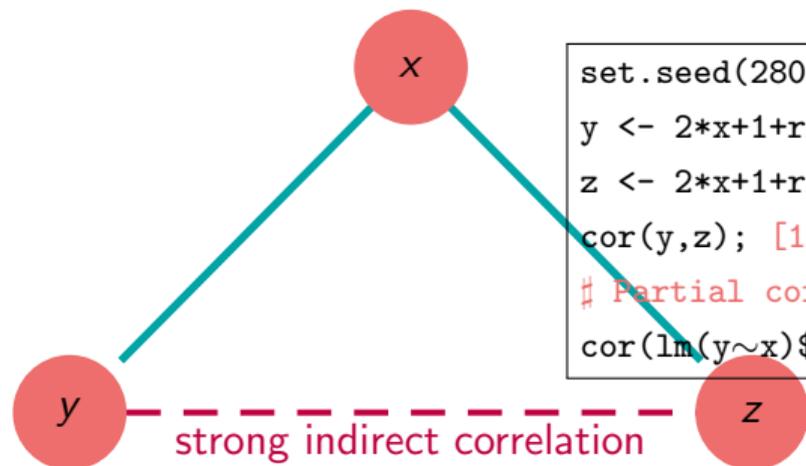
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> But correlation is not causality...



```
set.seed(2807); x <- runif(100)
y <- 2*x+1+rnorm(100,0,0.1); cor(x,y); [1] 0.9988261
z <- 2*x+1+rnorm(100,0,0.1); cor(x,z); [1] 0.998751
cor(y,z); [1] 0.9971105
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# Partial correlation
cor(lm(y~x)$residuals, lm(z~x)$residuals) [1] -0.1933699
```

> Partial correlation is also...

For: $(X_i)_{i=1,\dots,n}$ i.i.d. $\mathcal{N}(0, \Sigma)$ (gene expressions)

▶ $\text{Cor} \left(X^j, X^{j'} \mid (X^k)_{k \neq j, j'} \right)$

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- ▶ Related to $\beta_{jj'}$ in linear regression models:

$$X^j = \sum_{j' \neq j} \beta_{jj'} X^{j'} + \epsilon_j$$

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[Meinshausen and Bühlmann, 2006]

> Why restrict yourself at linear regression?

- ▶ GGM: Gaussian assumption + fit of p linear regressions

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Problems: ill-conditioned, only linear dependencies, restricted to Gaussian case.

- ▶ Just fit p regressions!

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But: Direct dependency interpretation is lost.



> My favorite regression method? Random forest!

[Huynh-Thu et al., 2010] **GENIE3**



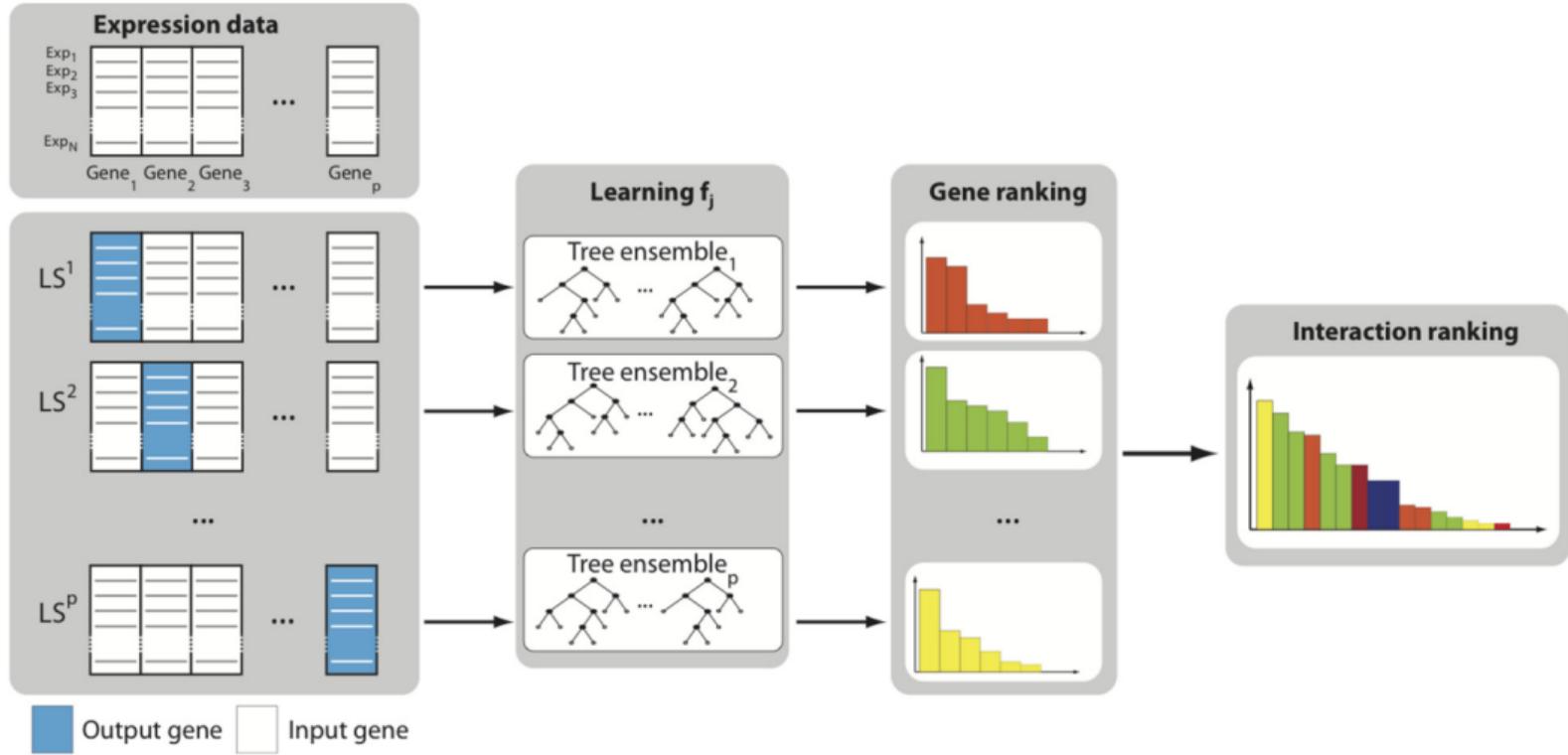
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➤ GENIE3: Using feature selection in RF to predict edges



> Important notes: orientation

Notation: $w_{jj'}$ weight obtained by $X^{j'}$ to predict X^j

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- ▶ in general $w_{jj'} \neq w_{j'j}$ which gives a way to obtain **oriented edges** (not really causality though)



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$$\sum_{\mathcal{N} \text{ defined by } j'} \left[|\mathcal{N}| \text{Var} \left(X_{\mathcal{N}}^j \right) - |\mathcal{N}_R| \text{Var} \left(X_{\mathcal{N}_R}^j \right) - |\mathcal{N}_L| \text{Var} \left(X_{\mathcal{N}_L}^j \right) \right]$$

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Advantages:

- ▶ **fast** to compute (compared to MDA obtained by permutation)
- ▶ RF can be replaced by **Extra-Trees** ensemble Pierre's Thursday class

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Drawback:

- ▶ might be **slightly less efficient** than MDA

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- ▶ output: ranking of the edges based on $(w_{jj'})_{j,j':j \neq j'}$ ⇒ edges require a threshold



➤ Experiments on *Escherichia coli*

- ▶ expression data: $n = 907$, $p = 4297$ (microarray)
- ▶ “ground truth” network: from RegulonDB (curated but might not be exhaustive; 1471 genes only)



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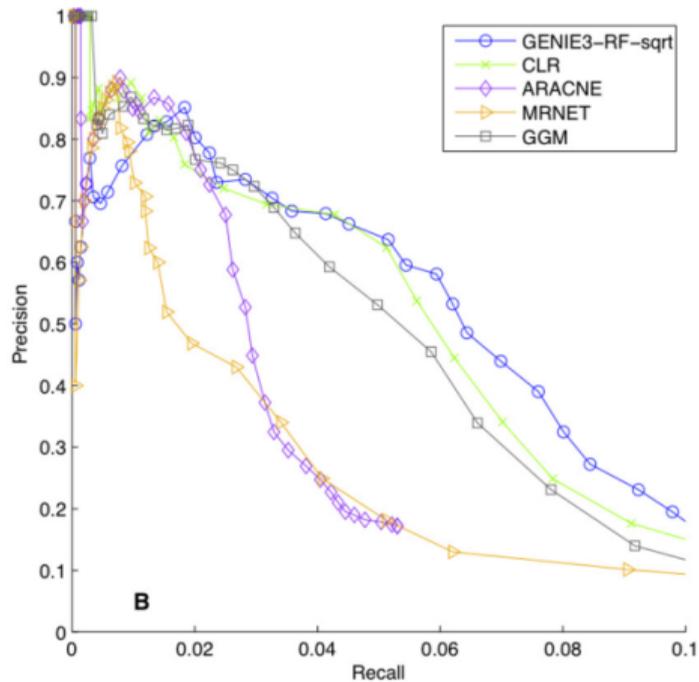
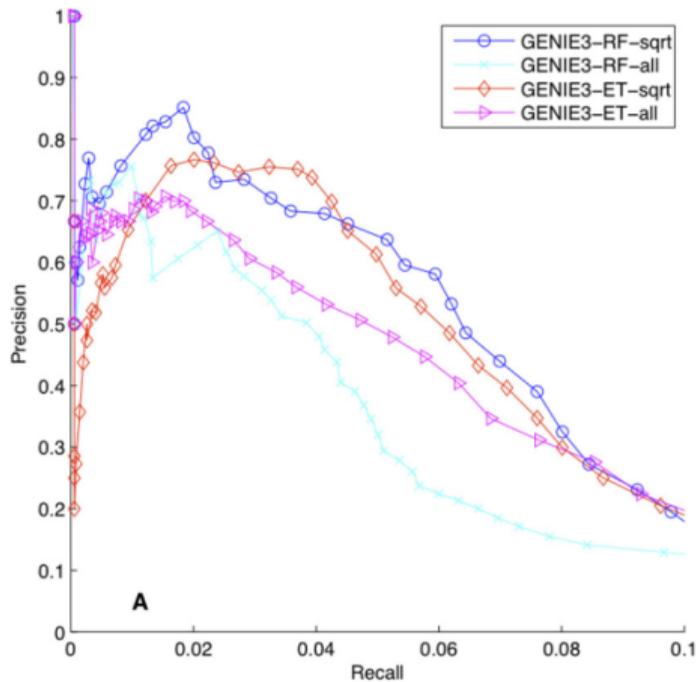
Hyper-parameters:

- ▶ # trees: 1,000
- ▶ $m = \sqrt{p-1}$ or $p-1$ (full)
- ▶ RF or ET
- ▶ no decision on edges (PR and ROC curves)
- ▶ sets of predictors restricted to **known regulators**

So: ranking of $(w_{jj'})_{j=1, \dots, p, j': \text{reg. only}}$.



Results



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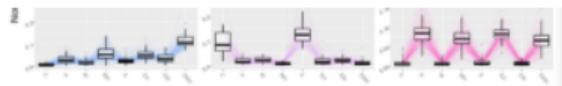
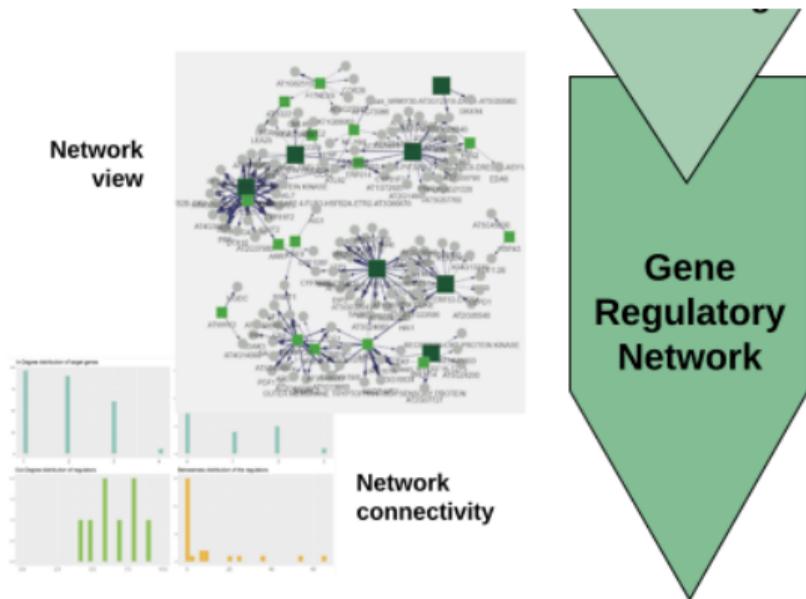
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DIANE: How to select edges? [Cassan et al., 2021]

<https://diane.bpmp.inrae.fr/>



GENIE3 GRN inference + edges testing
Interactive network exploration - statistics
Module detection and analysis (GO terms)

Gene community descriptions



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> What's new in **DIANE**?

1. predictors are only TF (transcription factors) **standard pre-filtering**
2. transcription factors (highly correlated) can be **grouped into a single gene**
3. **edges pre-selected** using **GENIE3** (threshold based on plausible global density)
4. **empirical p -value** computation based on MDA for final selection with **rfpermute** (using MDA)



➤ More on edge selection [Aibar et al., 2017]

SCENIC (oriented toward single-cell) / **GENIE3** component selects edges using:

1. $\text{weight} > 0.001$
2. further filters for multiple gene sets (a gene set = a cluster of genes with a TF):
 - ▶ top predicted genes for each TF
 - ▶ top predictor TF for each gene
 - ▶ several weight thresholds
3. further filtering (using biological information on DNA motifs with **RcisTarget**)
not described here



> More on tree ensemble methods [Aibar et al., 2017]

Alternative to **GENIE3** in **SCENIC**: **GRNBoost**

<https://github.com/aertslab/GRNBoost>

Replace RF method with XGBoost:

- ▶ tree ensemble based on boosting
- ▶ tree depth restricted to 1

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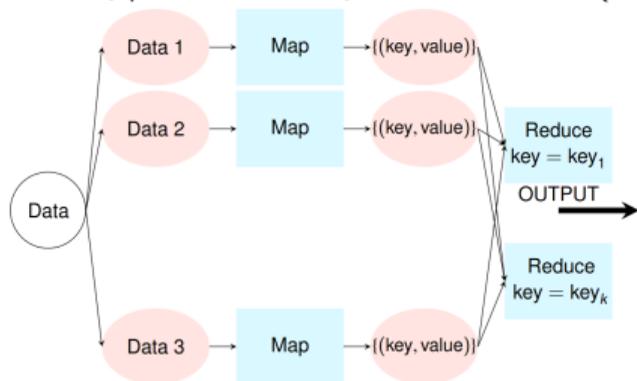
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Map/Reduce implementation (for spark):



- ▶ map split based on targets
- ▶ map output: set of edges (same filters) (**not 100% sure**)
- ▶ reduce: union of output edges

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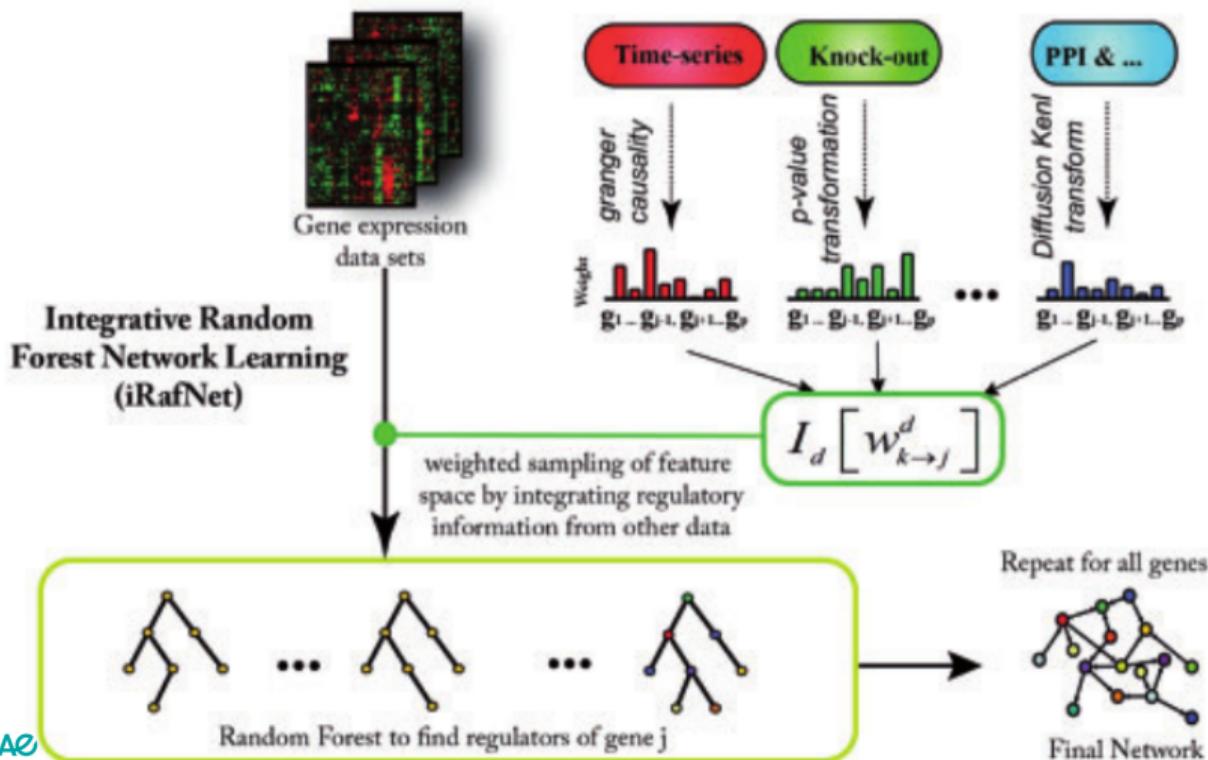
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Integration of knowledge into Random Forest [Petralia et al., 2015]

IRafNet

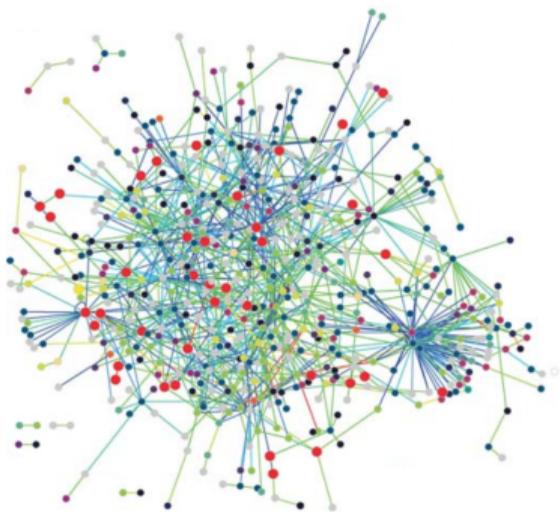


➤ Using prior knowledge as a weight

1. Knowledge (given): modelled by $(w_{jj'}^{\text{prior}})_{jj'}$
2. in RF_j , change the split rule definition:
 - ▶ sample $N \sim \mathcal{U}(\llbracket 1, p \rrbracket)$
 - ▶ sample N possible predictors with probability $(w_{jj'}^{\text{prior}})_{j'}$
 - ▶ find the best split among them



➤ Example of prior weights: Protein-Protein Interactions (PPI)

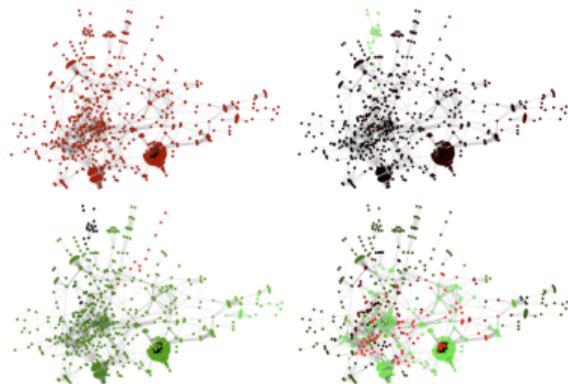
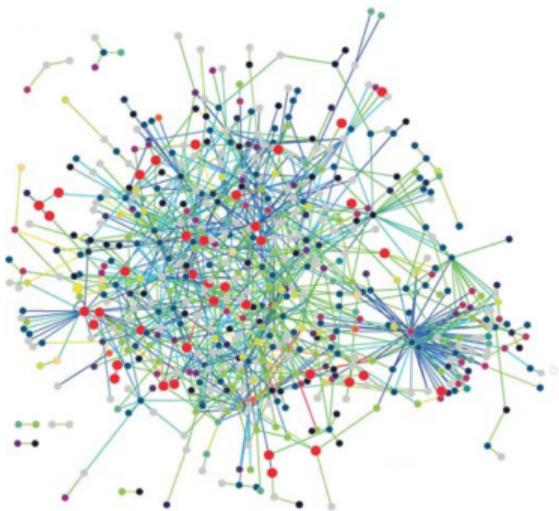


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1. from PPI network, Laplacian $L = D - P^{\text{PPI}}$ with $P_{jj'}^{\text{PPI}} \in \{0, 1\}$

Why? L eigendecomposition \sim graph structure

[Rapaport et al., 2007].

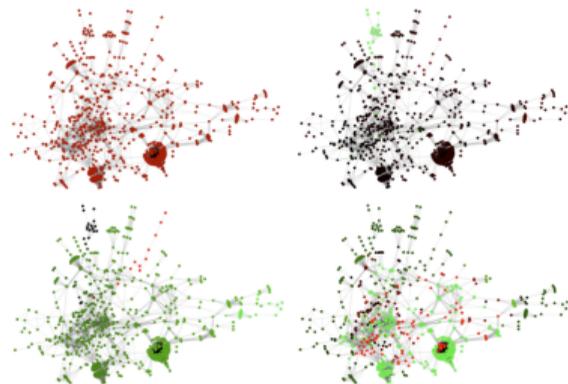


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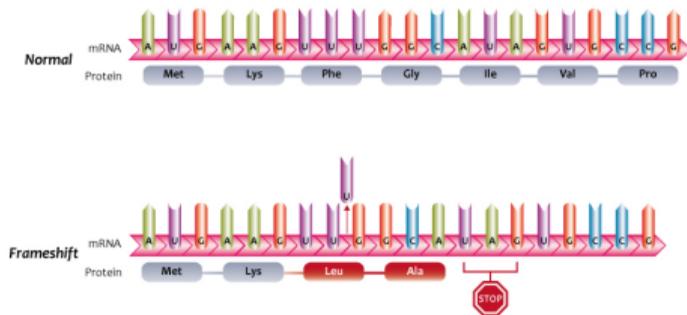
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2. $W^{\text{PPI}} = e^{-L}$ (heat kernel [Kondor and Lafferty, 2002])

Example of prior weights: knockouts

1. $\mathcal{K} \subset \llbracket 1, p \rrbracket$ knockouts
2. for $j \in \mathcal{K}$ and $j' \in \llbracket 1, p \rrbracket$, “ j affects j' ” if expression of j' is significantly different (Student's test) before/after knockout
 $w_{jj'}^{\text{KO}} := p\text{-value}$
3. weights for $j \notin \mathcal{K}$: weighed average $(w_{lj'}^{\text{KO}})_{l \in \mathcal{K}}$ using similarity of gene sets that affect j and l



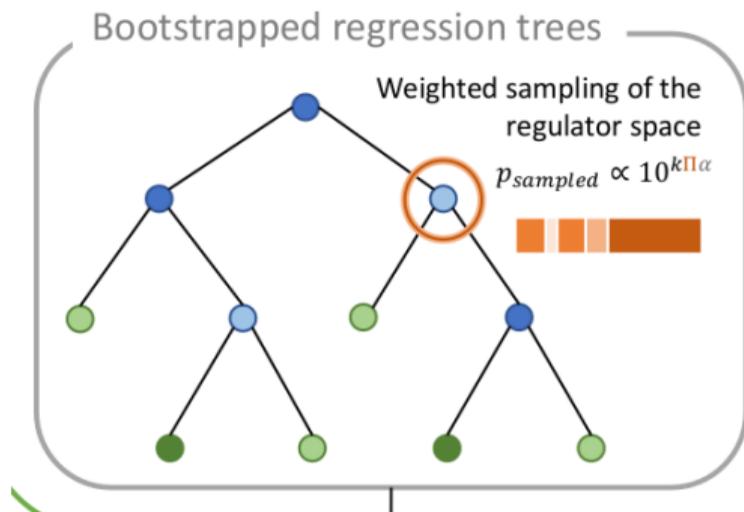
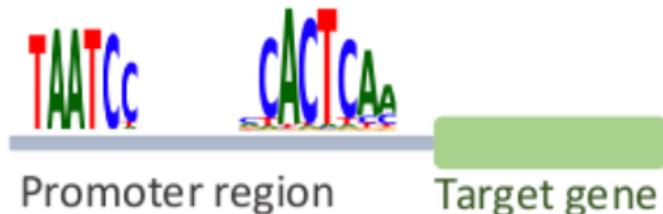
Adapted from Campbell NA (ed). Biology, 2nd ed, 1990.

Alternative ways to use priors (and alternative priors)

- ▶ using TFBS prior [Cassan et al., 2023]

TFBS prior matrix : Π

PWM occurrence score
in the target's promoter



➤ Alternative ways to use priors (and alternative priors)

- ▶ using TFBS prior [Cassan et al., 2023]

- ▶ using chromatine accessibility (ATAC-seq) **SCENIC+** [Bravo González-Blas et al., 2023] accessible regions + motif enrichment of these regions are used to pre-filter candidate enhancers



➤ Want to know more on network inference?

Some useful benchmarks:

- ▶ [Saint-Antoine and Singh, 2023]
- ▶ [Kang et al., 2021]
- ▶ [Hawe et al., 2019]
- ▶ [Marbach et al., 2012]: DREAM5 (simulated and real data)



End of the story!

Questions?



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> Credits

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- ▶ Image of **DIANE** network inference is taken from [[Cassan et al., 2021](#)]
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- ▶ Image of Laplacian eigenvector decomposition is taken from [[Rapaport et al., 2007](#)]
- ▶ Images of TFBS priors and weights is taken from [[Cassan, 2022](#)]

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(unofficial) Beamer template made with the help of Thomas Schiex, Matthias Zytnicki and Andreea Dreau:

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